### Physics 09-02 Resistance and Resistivity

# Another way to find resistance

| ······   |   |  |  |  |  |
|--|---|--|--|--|--|
| varies   | with  | and  | with   |  |  |
| (or cross-sectional                                | ) a wi  | ire  |  |  |  |
| Short, thick wire $\rightarrow$                    | resistance  |  |  |  |  |
| Long, skinny wire $\rightarrow$                    | resistance  | !  |  |  |  |
|  | $R = \frac{\rho L}{A}$  |  |  |  |  |
| ο <i>ρ</i> =                                       | _ (Unit: Ωm)  |  |  |  |  |
| • Table 20.1 lists resistivities of some materials |   |  |  |  |  |
| ◦ Metals $→$                                       | resistivity (1  | $\times 10^{-8} \Omega \mathrm{m}$ )   |  |  |  |
| ◦ Insulators $→$                                   | resisitivi  | ty (1 × 10 <sup>15</sup> $\Omega$ m)   |  |  |  |
| • Semi-conductors                                  | → re  | sistivity  |  |  |  |
|  | varies<br>(or cross-sectional<br>Short, thick wire →<br>Long, skinny wire →<br>$\circ  \rho =$<br>Table 20.1 lists resistivitie<br>$\circ $ Metals →<br>$\circ $ Insulators →<br>$\circ $ Semi-conductors | varies with) a with<br>(or cross-sectional) a with<br>Short, thick wire → resistance<br>Long, skinny wire → resistance<br>$R = \frac{\rho L}{A}$<br>$\circ \rho = (Unit: \Omega m)$<br>Table 20.1 lists resistivities of some materials<br>$\circ$ Metals → resistivity (1<br>$\circ$ Insulators → resistivity (1<br>$\circ$ Semi-conductors → resistivity | varieswithand<br>(or cross-sectional) a wire<br>Short, thick wire →resistance<br>Long, skinny wire →resistance<br>$R = \frac{\rho L}{A}$<br>$\circ  \rho = \(Unit: \Omega m)$<br>Table 20.1 lists resistivities of some materials<br>$\circ  Metals \rightarrow \resistivity (1 × 10^{-8} \Omega m)$<br>$\circ  Insulators \rightarrow \resistivity (1 × 10^{15} \Omega m)$<br>$\circ  Semi-conductors \rightarrow \resistivity$ |  |  |

#### Why are long wires thick?

Wire thicknesses are measured in gauges. 20-gauge wire is thinner than 16-gauge wire. If 20-gauge wire has  $A = 5.2 \times 10^{-7} m^2$  and 16-gauge wire has  $A = 13 \times 10^{-7} m^2$ , find the resistance per meter of each if they are copper.

| Table 20.2 Tempature Coeffici | ients of Resistivity $lpha$                | Silicon (pure) | 23 |
|-------------------------------|--|----------------|----|
| Material                      | Coefficient $\alpha$ (1/°C) <sup>[2]</sup> | Silicon        | 0. |
| Conductors                    |  | Insulators     |    |
| Silver                        | $3.8 \times 10^{-3}$                       | Amber          | 5> |
| Copper                        | 3.9×10 <sup>-3</sup>                       | Glass          | 10 |
| Gold                          | 3.4×10 <sup>-3</sup>                       | Lucite         | >1 |
| Aluminum                      | 3.9×10 <sup>-3</sup>                       | Mica           | 10 |
| Tungsten                      | 4.5×10 <sup>-3</sup>                       | Quartz (fused) | 75 |
| Iron                          | 5.0×10 <sup>-3</sup>                       | Rubber (hard)  | 10 |
| Platinum                      | 3.93×10 <sup>-3</sup>                      | Sulfur         | 10 |
| Lead                          | 3.9×10 <sup>-3</sup>                       | Teflon         | >1 |
| Manganin (Cu, Mn, Ni alloy)   | $0.000 \times 10^{-3}$                     | Wood           | 10 |
| Constantan (Cu, Ni alloy)     | $0.002 \times 10^{-3}$                     |                |    |
| Mercury                       | $0.89 \times 10^{-3}$                      |                |    |
| Nichrome (Ni, Fe, Cr alloy)   | $0.4 \times 10^{-3}$                       |                |    |
| Semiconductors                |  |                |    |
| Carbon (pure)                 | $-0.5 \times 10^{-3}$                      |                |    |
| Germanium (pure)              | $-50 \times 10^{-3}$                       |                |    |
| Silicon (pure)                | $-70 \times 10^{-3}$                       |                |    |

### **Resistivity and Temperature**

 $\rho = \rho_0 (1 + \alpha \Delta T)$ 

- $\rho$  = resistivity at temperature *T*
- $\rho_0$  = resistivity at temperature  $T_0$
- *α* = temperature coefficient of resistivity (Unit: 1/°C (or 1/K))

Metals

• Resistivity \_\_\_\_\_\_ with temperature

• α is \_\_\_\_\_

- Semiconductors
  - Resistivity \_\_\_\_\_\_ with temperature
  - α is \_\_\_\_\_

## **Resistance and Temperature**

 $R = R_0(1 + \alpha \Delta T)$ 

- *R* = resistance at temperature T
- *R*<sub>0</sub> = resistance at temperature T<sub>0</sub>
- $\alpha$  = temperature coefficient of resistivity (Unit: 1/°C (or 1/K))

A heating element is a wire with cross-sectional area of  $2 \times 10^{-7}$  m<sup>2</sup> and is 1.3 m long. The material has resistivity of  $4 \times 10^{-5} \Omega m$  at 200°C and a temperature coefficient of  $3 \times 10^{-2} 1/°$ C. Find the resistance of the element at 350°C.

#### Name:

| Material                      | Resistivity $\rho$ ( $\Omega$ · m |
|-------------------------------|-----------------------------------|
| Conductors                    |                                   |
| Silver                        | 1.59×10 <sup>-8</sup>             |
| Copper                        | $1.72 \times 10^{-8}$             |
| Gold                          | 2.44×10 <sup>-8</sup>             |
| Aluminum                      | 2.65×10 <sup>-8</sup>             |
| Tungsten                      | 5.6×10 <sup>-8</sup>              |
| Iron                          | 9.71×10 <sup>-8</sup>             |
| Platinum                      | 10.6×10 <sup>-8</sup>             |
| Steel                         | 20×10 <sup>-8</sup>               |
| Lead                          | 22×10 <sup>-8</sup>               |
| Manganin (Cu, Mn, Ni alloy)   | 44×10 <sup>-8</sup>               |
| Constantan (Cu, Ni alloy)     | 49×10 <sup>-8</sup>               |
| Mercury                       | 96×10 <sup>-8</sup>               |
| Nichrome (Ni, Fe, Cr alloy)   | 100×10 <sup>-8</sup>              |
| Semiconductors <sup>[1]</sup> |                                   |
| Carbon (pure)                 | 3.5×10 <sup>5</sup>               |
| Carbon                        | $(3.5-60) \times 10^5$            |
| Germanium (pure)              | 600×10 <sup>-3</sup>              |
| Germanium                     | $(1-600) \times 10^{-3}$          |
| Silicon (pure)                | 2300                              |
| Silicon                       | 0.1-2300                          |
| Insulators                    |                                   |
| Amber                         | 5×10 <sup>14</sup>                |
| Glass                         | $10^9 - 10^{14}$                  |
| Lucite                        | >10 <sup>13</sup>                 |
| Mica                          | $10^{11} - 10^{15}$               |
| Quartz (fused)                | 75×10 <sup>16</sup>               |
| Rubber (hard)                 | $10^{13} - 10^{16}$               |
| Sulfur                        | 1015                              |
| Teflon                        | >10 <sup>13</sup>                 |
| Weed                          | 108 1011                          |

| Physics 09-02 Resistance and Resistivity | Name:                                      |  |
|--|--|--|
| Superconductors                          |  |  |
| Materials whose =                        |  |  |
| become superconductors at                | temperatures                               |  |
| <ul> <li>Some materials using</li> </ul> | work at much temperatures                  |  |
| No current                               |  |  |
| • Used in                                |  |  |
| <ul> <li>Transmission of,</li> </ul>     | ,, Powerful, small electric motors, Faster |  |
| chips                                    |  |  |

#### Homework

- 1. In which of the three semiconducting materials listed in Table 20.1 do impurities supply free charges? (Hint: Examine the range of resistivity for each and determine whether the pure semiconductor has the higher or lower conductivity.)
- 2. Does the resistance of an object depend on the path current takes through it? Consider, for example, a rectangular bar–is its resistance the same along its length as across its width? (See Figure.)
- 3. If aluminum and copper wires of the same length have the same resistance, which has the larger diameter? Why?
- 4. What is the resistance of a 20.0-m-long piece of 12-gauge copper wire having a 2.053-mm diameter? (OpenStax 20.24) 0.104 Ω
- 5. The diameter of 0-gauge copper wire is 8.252 mm. Find the resistance of a 1.00-km length of such wire used for power transmission. (OpenStax 20.25) **0.322**  $\Omega$
- 6. If the 0.100-mm diameter tungsten filament in a light bulb is to have a resistance of 0.200  $\Omega$  at 20.0 °C, how long should it be? (OpenStax 20.26) **2.81** × 10<sup>-2</sup> m
- 7. What current flows through a 2.54-cm-diameter rod of pure silicon that is 20.0 cm long, when  $1.00 \times 10^3$  V is applied to it? (Such a rod may be used to make nuclear particle detectors, for example.) (OpenStax 20.28) **1**. **10** × **10**<sup>-3</sup> **A**
- 8. (a) To what temperature must you raise a copper wire, originally at 20.0 °C, to double its resistance, neglecting any changes in dimensions? (b) Does this happen in household wiring under ordinary circumstances? (OpenStax 20.29) 276 °C
- 9. A resistor made of Nichrome wire is used in an application where its resistance cannot change more than 1.00% from its value at 20.0 °C . Over what temperature range can it be used? (OpenStax 20.30) –5°C to 45 °C
- 10. Of what material is a resistor made if its resistance is 40.0% greater at 100 °C than at 20.0 °C? (OpenStax 20.31)
   5.00 × 10<sup>-3</sup> /°C
- (a) Of what material is a wire made, if it is 25.0 m long with a 0.100 mm diameter and has a resistance of 77.7 Ω at 20.0 °C?
  (b) What is its resistance at 150 °C? (OpenStax 20.33) 1.1 × 10<sup>2</sup> Ω
- 12. (a) Digital medical thermometers determine temperature by measuring the resistance of a semiconductor device called a thermistor (which has  $\alpha = -0.0600 / ^{\circ}C$ ) when it is at the same temperature as the patient. What is a patient's temperature if the thermistor's resistance at that temperature is 82.0% of its value at 37.0 °C (normal body temperature)? (OpenStax 20.37a) **40.0** °C